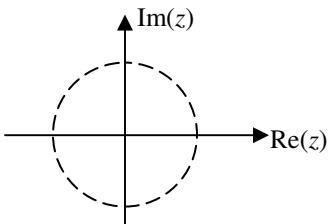
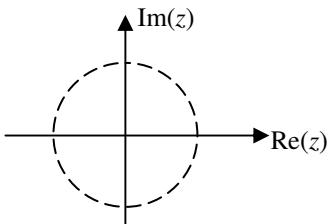


1. Plot the sixth roots of -1 in the argand diagram below.



3. Show that $\sqrt[6]{-1} = \sqrt[3]{\pm i}$.

2. Plot the cube roots of i and $-i$ in the argand diagram below.



5. Factorise $z^2 - i$.

6. Factorise $z^2 + i$.

7. Factorise $z^3 - (3+i)z^2 + z - 3 - i$.

8. Factorise $z^3 + 1$.

9. Factorise $z^4 - 16$.

10. Factorise $z^4 + 4$.

11. Factorise $z^6 - 64$.

Numerical, algebraic and worded answers.

$$\begin{aligned}
 3. (-1)^{(1/6)} &= ((-1)^{(1/2)})^{(1/3)} \\
 &= (\pm i)^{(1/3)} \\
 4. \text{cis}(\pi/5), \text{cis}(3\pi/5), \text{cis}(\pi), \\
 &\text{cis}(-\pi/5), \text{cis}(-3\pi/5) \\
 5. (z-1/\sqrt{2}-i/\sqrt{2}) (z+1/\sqrt{2}+i/\sqrt{2}) \\
 6. (z+1/\sqrt{2}-1/\sqrt{2}i) (z-1/\sqrt{2}+1/\sqrt{2}i) \\
 7. (z-i)(z+i)(z-3-i) \\
 8. (z+1)(z-1/2-i\sqrt{3}/2)(z-1/2+i\sqrt{3}/2) \\
 9. (z-2)(z+2)(z-2i)(z+2i) \\
 10. (z-1-i)(z-1+i)(z+1-i)(z+1+i) \\
 11. (z-2)(z+2)(z+1-\sqrt{3}) \\
 &\quad (z+1+\sqrt{3})(z-1-\sqrt{3})(z-1+i\sqrt{3})
 \end{aligned}$$