1. Use vectors to prove that the diagonals of a rhombus are perpendicular.
2. Use vectors to prove the cosine rule.

3. Use vectors to prove that the angle subtended by the diameter of a semi-circle is a right angle.
4. If two linearly independent vectors are of equal magnitude, prove that their sum is perpendicular to their difference.

5. P, Q and R are points of trisection of sides $\mathrm{AB}, \mathrm{AC}$ and BC respectively. Use vectors to show that BPQR is a parallelogram.

6. Use vectors to show that any two medians of a triangle trisect each other.

7. Given $\overrightarrow{O A}=10 \mathbf{a}, \overrightarrow{O B}=6(\mathbf{a}+\mathbf{b})$ and $\overrightarrow{O C}=15 \mathbf{b}$. Show that points $A, B$ and $C$ are collinear.

8. ABCD is a parallelogram. M is the midpoint of AB . Use vectors to show that DM and AC trisect each other.

9. Use vectors to show that any two body diagonals of a parallelepiped bisect each other.

10. Use vectors to prove that the midpoints of the sides of a quadrilateral are the vertices of a parallelogram.

